

# Intensively Computational Electromagnetic Techniques for the Analysis of Complex Communication Devices

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  - Integral equation with free-space Green's functions
  - Integral equation with complex Green's functions

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  - Shielded Microwave Filter
  - Fields Calculation for Multipactor Analysis

- 4 Conclusions



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- CAD tools can decrease development time and cost, by reducing experimental work.
- **Problem:**
- Usually, practical designs require hundreds of time consuming analysis:
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#### Numerical approach

- ☞ Faster and larger computers.
- ☞ Parallel computation to exploit the computational capabilities of the machines.
- ☞ Research into numerical routines to invert faster larger systems (iterative solvers, etc.).

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#### Cavity Green's functions

- ☞ More intelligent Kernel.
- ☞ The enclosure and dielectric substrates are already included in the Kernel.
- ☞ Numerical solution is reduced

# Integral equation with free-space Green's functions

## Theory

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- ☞ Only exponential functions are involved.
- ☞ It has only information on the radiation condition at infinity.
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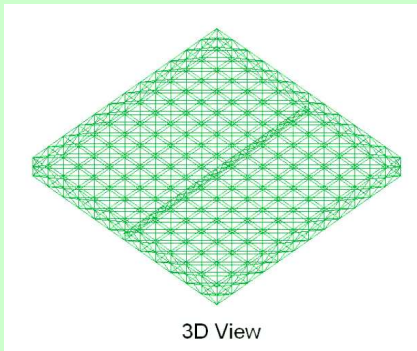
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- Green's functions do not contain information on dielectric substrates.
- For printed structures the dielectrics must also be discretized, either in volume (VIE) or in surface (SIE).
- Huge systems of linear equations must be solved fast.



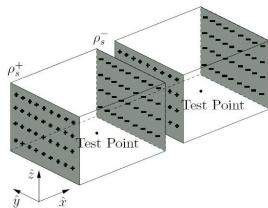


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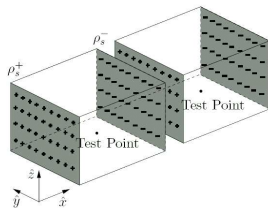
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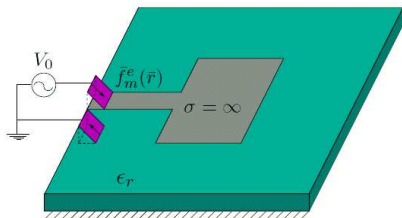
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- For rectangular shaped cavities, analytical solutions in terms of series are available.
- Mathematical transformations to improve convergence are appropriate (Kummer, Ewald).



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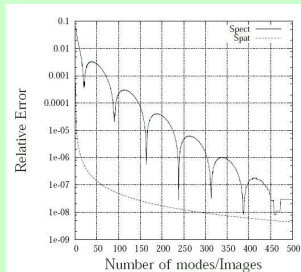
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- Boundary conditions are imposed at discrete points along the cavity wall.



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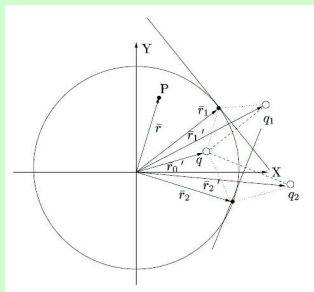
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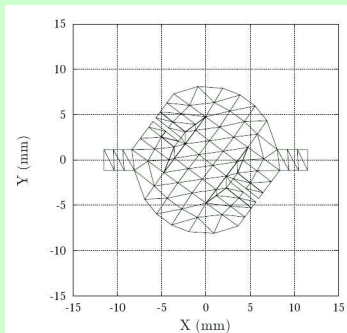
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### Design of Shielded Microwave Filters

- A CAD tool based on these techniques can be very useful in the design of practical circuits for communication systems (mobile, satellite, etc).
- The CAD tool will be useful only if analysis time can be reduced even for complex structures.



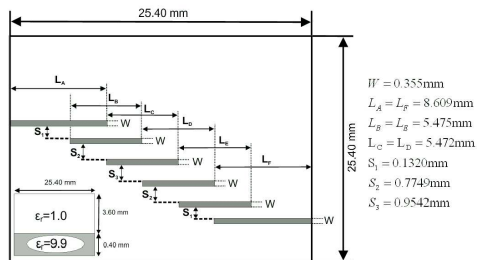


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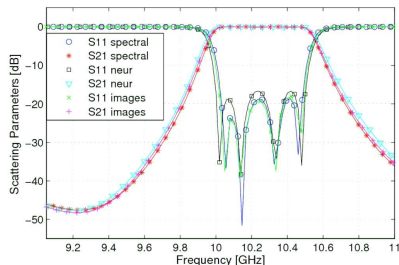
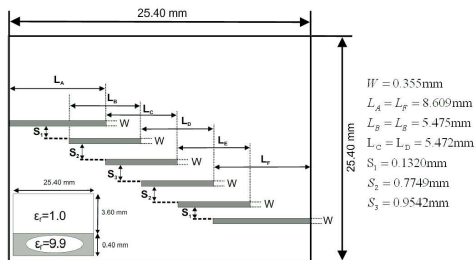


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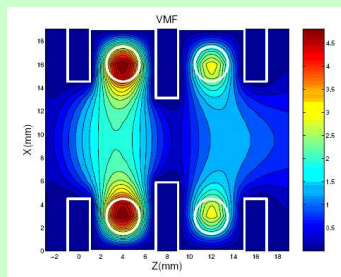
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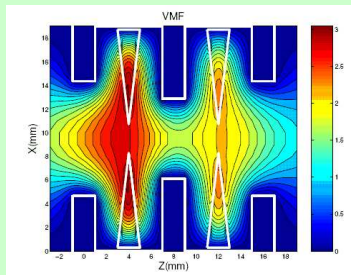
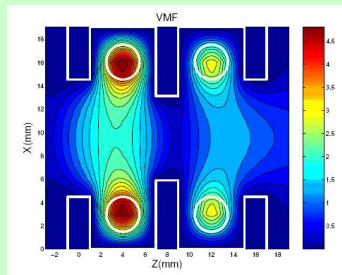


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- Which of the two approaches is most suited for available techniques?.